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# **ORIGINAL ARTICLE**

# Determination of A Some Simple Methods for Outlier Detection in Maximum Daily Rainfall (Case Study: Baliglichay Watershed Basin – Ardebil Province – Iran)

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# ABSTRACT

Outliers in maximum daily rainfall can play a considerable role in unreal analysis leading to unreal predictions. Therefore, accurate statistical determination of data to find outliers is very important. In the present work, data related to maximum daily rainfall obtained from 12 rain gauge stations belonging to Regional Water Corporation of Ardebil Province inside and around Baliglichay watershed basin were used. Five methods for outlier detection (namely 3×SD±M, Box-Whisker Plot, American Water Resources Association, Grubbs' Test, and Mahalanobis Distance) were adopted. After detecting outliers by the mentioned methods, three control stations were considered in terms of distance, location, and climate. The control stations consisted of 9 rain gauge stations for regional water and 5 meteorological rain gauge stations. Afterwards, outliers in each station were controlled by simultaneous data achieved from the control stations through the five mentioned methods. The results obtained from the present study revealed that only 5 out of 14 outliers detected in 3 out of 7 stations were confirmed. Furthermore, comparison of performance of the methods showed that American Water Resources Association and 3×SD±M methods were more efficient to detect outliers while Mahalanobis Distance).

Keywords: Baliglichay watershed, Grubb's Test, American Water Resources Association, maximum daily rainfall, outlier.

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## INTRODUCTION

Description of meteorological variables such as heavy rainfall is cumbersome due to haphazard climatic variations and sampling error in limited data as a small sample belonging to an indefinitie statistical population [21]. Maximum daily rainfall is a meteorological parameter with highly haphazard nature compared with rainfall data such as monthly and annual rainfall [8]. Adoption of maximum rainfall in estimation of flood and amount of runoff in small or without long-term hydrometric data regions have long been in center of attention. According to the relations provided by SCS, hourly rainfall can be estimated from maximum daily rainfall with varying turnover times. The relations are very important in estimation of hydrographs. With regard to lack of data related to short-term rainfall in many parts of the world, estimation of such information is performed through the methods concerning maximum daily rainfall [4]. Several application for annual maximum daily rainfall with varying turnovers can somewhat reflect importance of such rainfall. Therefore, before calculations of floods and designing water structures, more precise daily rainfall data in terms of existence of outliers is necessary. An outlier can be considered an observation which abnormally or haphazardly deviates from normal status of data and analysis [1]. As a matter of fact, one of necessary factors in abundance analysis is existence of real and long-term data where outliers may have considerable adverse effect in data prediction [3]. Such effect leads to unreal estimations in data analyses for a given variable; for instance:

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- (1) Outliers lead to unreal probabilistic distribution;
- (2) Estimation of probabilistic distributions parameters is influenced by outliers leading to faulty estimation;
- (3) Low outliers cause underestimation leading to structure collapse in big floods;
- (4) High outliers cause overestimation leading to higher costs of water structures building (2).

Thus, false inputs result in false outputs so that an outlier in some statistical methods can specify final results [6]. Severalmethods have been proposed for outlier detection, none of which have been globally accepted [18]. Such methods as main attribute [9,11], multivariable regression and artificial network [16], genetic algorithm [25], and Mahalanobis Distance-based method[19,20] were presented with the last one as being the most famous (15). Some Iranian authors have performed studies on effect of outliers in such fields as hydrology and sedimentology. For instance, (3) evaluated effect of outliers in hydrologic abundance analusis by use of linear torque method in Jiroft Dam region in Iran on annual maximum rainfall series and concluded that outliers have no influence on regional distribution; however, they were found to exert a considerable effect on determination of the most suitable statistical distribution for data relating to a station.[6] adopted main attributes method in order to detect outliers in regional analysis of flood in Lake Urmia region in Iran and found that this method has high precision. [2] used univariate detection methods such as 3×SD±M, median ± outliers median, Box-Whisker Plot, and Grubbs' Test and concluded that median ± outliers median and Box-Whisker Plot are more efficient than 3×SD±M and Grubbs' test. Many of these methods need a lot of calculations and time and are not computable by statistical software. Therefore, more than one method can be adopted for outlier selection to assure higher accuracy. On this basis, five simple methods were used in the present study in order to detect outliers in maximum daily rainfall data in the stations located in and around Baliglichay watershed in northwest of Iran.

# MATERIALS AND METHODS

### Stations and the region

Baliglichay watershed is one of subsidiary regions of Gharasou watershed basin located in Pol-e-Almas hydrometric station (2014 m high and 1036.18 km<sup>2</sup>) 85% of which s located in Ardebil Province and the rest in located in Eastern Azerbaijan Province. Baliglichay River originates from Sabalan Mountain in northwest and Bozghoosh in the south. The river is one of the most important rivers in northwest of Iran as it flows through Ardebil City and it is considered as the source of drinking and agricultural water. In order to detect outliers in maximum daily rainfall data, data related to 12 rain gauge stations with a 27-year statistical term (1983-2009) were used because of proper distribution of the station; location of the stations and Baliglichay watershed were depicted in Fig. 1.



Figure 1: Location of Baliglichay watershed and distribution of the stations

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Outlier detection methods

Outlier detection methods can be generally divided into three groups: univariate, two-variate, and multivariate detection methods. Multivariate outlier detection method consists of multivariate determination of each observation according to a blend of variables. Also, there are various methods in order to perform univariate outlier detection which can be classified into range and statistical tests. in range methods, observations distribution is determined and data out of a given range are considered outliers; in statistical methods, all outlier detection methods are based upon the principle that an outlier is a doubtful observation which is somewhat or fully out of the subject because the data were not made by hypothetical models of random variable [7,10]. In the present work, the univariate methods 3×SD±M. Box-Whisker Plot, American Water Resources Association, Grubbs' Test, and Mahalanobis Distance were adopted so as to detect outliers. After performing calculation of each method and detection of outliers in maximum daily rainfall data, the nearest stations' data were adopted in order to assure correctness of outliers where for each station with outliers, 3 control station were assigned in terms of the nearest distance, location, and climate. Rainfall data for 9 rain gauge stations for regional water and 5 meteorological rain gauge stations were considered as control stations. In order to make suitable decision, the data exceeding the lower threshold were eliminated from outliers [5]. Then, high outliers were compared with the nearest stations. When there were similar simultaneous data in control stations, the data were not regarded as outliers and introduced into maximum daily rainfall data; otherwise, they were considered as outliers. This way, performance of outlier detection methods was compared. 3×SD±M

One of the most important and well-known univariate outlier detection methods is 3×SD±M. this conventional method is based upon the principle that first, data mean and 3×SD are obtained; then, data higher than 3×SD+M or lower than 3×SD-M are regarded as outliers and eliminated from data set [28]. Box-Whisker Plot

The method is widely used in order to detect outliers [20,18]. Box-Whisker is a plot presenting dataset very effectively by aid of central and distribution criteria. The plot was proposed by famous statistician Tukey [24]. Box plot is a method for summarizing estimated data according to a distance index which is adopted for discovering properties and data analysis [10]. In this method, a rectangle (box) and two lines around the rectangle (whisker) are used and the plot is drawn by median, the first and third quarters, and the lowest and highest observed amount. The rectangle length equals interquartile range (IQR= Q3- Q1). Internal and external frontiers are specified by successive steps. When a data is placed between internal and external boundaries, it is called weak outliner (data smaller than Q1-1.5IQR and bigger than Q1+1.5 IQR) and if it is placed out of the external boundaries, it is regarded as strong outliner (data smaller than Q1-3IQR and bigger than Q1+3 IQR).

# 2-2-3- Grubbs' Test

The test was invented by Grubbs to detect outliers. In this method, the test has a statistic for each data obtained by the formulae mentioned by Grubbs and then compared with standard amount of each data. If it exceeds the standard, it is considered an outlier (14). There are two hypotheses in this test; null hypothesis is there is no outlier and the other hypothesis is there is at least one outlier. Statistic of this test (G) is derived as follows (23,14):

$$G = \frac{\max\left|x_i - \overline{x}\right|}{S} \tag{1}$$

where  $x_1$ ,  $x_2$ , and S stand for the biggest or smallest data, data mean, and standard deviation, respectively; the null hypothesis is rejected when the following relation is achieved:

$$G > \frac{(n-1)}{\sqrt{n}} \sqrt{\frac{t^2}{(\frac{q}{2n,n-2})}}$$
(2)

where *n* and  $t^2_{(a'_{2n,n-2})}$  stand for sample size and critical amount of t-student distribution statistic with

freedom degree of n-2 and significance level of  $\frac{a}{2n}$  ( $\alpha$ =0.05), respectively.

# 2-2-4- American Water Resources Association

This method was first proposed by American Water Resources Association and used for elimination of outliers. In this method, data kurtosis is obtained; if kurtosis exceeds +0.4, the test is done for high outliers and vice versa. If kurtosis is between the two ranges, the tests for both high and low outliers are performed. Detecting high and low outliers are done via the relations 3 and 4, respectively (5).

$$y_H = \overline{y} + k_N s_y \tag{3}$$

$$y_L = \overline{y} - k_N s_y \tag{4}$$

where  $y_{H_i} y_{L_i} \bar{y}_i$ ,  $S_{y_i}$  and  $k_N$  stand for high outliers' decimal logarithm, low outliers' decimal logarithm, data mean logarithm, SD of data logarithm, outliers abundance coefficient, respectively;  $k_N$  is derived as follows at significance level of 10% and 10<samples<150:

$$k_N = -3.62201 + 6.23446N^{.25} - 2.47832N^{.5} + 0.491436N^{.75} - 0.037911N$$
(5)

2-2-5- Mahalanobis Distance

Mahalanobis Distance acts as a criterion of multidimensional location of each observation relative to centroid of all bservations; in other words, the distance is a criterion of distance between each observation in multidimensional space and mean center of all observations. Advantage of Mahalanobis Distance compared to other distances is its considering covariance matrix (12). For a p-dimensional multivariate sample, Mahalanobis Distance for *i*<sup>th</sup> observation is obtained as follows:

$$MD_{i} = (x_{i} \ \bar{x})^{T} c^{-1} (x_{i} \ \bar{x})^{\frac{1}{2}} N$$
(6)

where  $x_i$ ,  $\vec{x}_i$ , and c stand for variables' vector for  $i^{\text{th}}$  observation, mean variables' vector (centroid of observations), and sample covariance matrix, respectively.

# **RESULTS AND DISCUSSION**

The results showed that 7 out of 12 stations suffered from outliers. Figures 2 and 3 depict the results obtained from Box-Whisker Plot and Mahalanobis Distance methods, respectively. Also, Table 1 summarized the results acquired from all five methods. The findings indicate that each method had a different outcome for outlier detection;  $3\times$ SD±M and American Water Resources Association methods detected the lowest outliers (one high outlier and 5 low outliers) while Box-Whisker Plot detected the most outliers (9high outliers). The methods used in the present study detected 14 outliers (10 high and 4 low outliers) altogether. After specifying the stations suffering from outliers, characteristics of these stations (stations of origin) along with control stations are presented in Table 2 and Figure 4.



Figure 2: the results obtained from Box-Whisker Plot in the stations with outliers

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Figure 4: the results acquired from Mahalanobis Distance in the stations Table 2: The calculated outliers for maximum daily rainfall by all the 5 methods in the stations

	3×SD±M		Box-Whisker Plot		American Water Resources Association		Grubbs' Test		Mahalanobis Distance	
Station	High outlier	Low outlier	High outlier	Low outlier	High outlier	Low outlier	High outlier	Low outlier	High outlier	Low outlier
Mola Ahmad	-	8.5	-	-	-	8.5	-	-	-	-
	-	7	-	-	-	7	-	-	-	7
	-	8	-	-	-	8	-	-	-	-
	-	-	50	-	-	-	50	-	-	-
Ardebil	-	2.9	-	-	-	2.9	-	2.9	2.9	2.9
	-	-	-	-	-	-	-	-	44.8	-
Lay	-	-	40	-	-	-	-	-	-	-
	-	-	44	-	-	-	44	-	44	-
Shams Abad	-	-	46	-	-	-	46	-	46	-
Almas	-	-	60	-	-	-	-	-	-	-
	65	-	65	-	65	-	65	-	-	-
Samian	-	-	44	-	-	-	-	-	-	-
	-	-	48	-	-	-	48	-	48	-
MeshkinShahr	-	-	48	-	-	-	48	-	-	-
Outliers	1	1	9	3	1	1	6	1	5	2

Table 3: Characteristics of the stations with outliers (stations of origin) and control stations

Station of origin Altitude (m)		Control stations Station type		Distance (km)	Altitude (m)	
Mola Ahmad		KozehTopragi	Regional water	8.15	1402	
	1512	Shams Abad	Regional water	8.9	1534	
		Almas	Regional water	12	1480	
		Almas	Regional water	11.4	1480	
Ardebil	1365	Gilandeh	Regional water	11.4	1341	
		KozehTopragi	Regional water	14	1402	
Lay		Nir	Regional water	12.8	1623	
	2038	Atashgah	Regional water	17.1	1778	
		Kalur	Regional water	21	1576	
Shams Abad		Koraim	Regional water	5.3	1534	
	1534	Mola Ahmad	Regional water	8.9	1512	
		Foladlu	Regional water	7.2	1473	
		Ardebil	Regional water	11.4	1365	
Almas	1480	KozehTopragi	Regional water	15	1402	
		Nir	Regional water	20	1623	
		Gilandeh	Regional water	12.6	1341	
Samian	1286	Ardebil	Regional water	16.2	1365	
		Namin	Regional water	21.3	1405	
		West Meshkin	Regional water	10	1244	
MeshkinShahr	1485	East Meshkin	Regional water	22	1211	
		Mashiran	Regional water	32	705	

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Figure 4: the stations with outliers (stations of origin) and control stations

The results obtained from the comparison of stations of origin and control stations (Table 3) indicate that out of 14 outliers detected in 7 stations by the five methods, only 5 outliers related to three stations (namely Mola Ahmad, Ardebil, and Almas) are confirmed because statistical determination of control stations showed that rainfall rates in 9 cases were close to detected outliers in stations of origin. Therefore, the data are of historical data for the stations and they cannot be considered as outliers. In order to determine efficiency of the methods, the ratios of detected outliers to real outlier (real percentage) and also to unreal outliers were measured for each method.

Table 3: the results obtained from determination of outlier detection for maximum daily rainfall relative to data obtained from control stations

Station	Occurrence date	Outlier	Control station 1	Control station 2	Control station 3
Mola Ahmad	1988//3	8.5	2	-	10
	1992//25	50	19	25	30
	1993//14	7	-	-	-
	1991//28	8	-	-	4
Ardebil	2007//2	2.9	-	-	-
	2001//25	44.8	30	28	27
Lay	1998//23	40	32	-	35
	2001//25	44	37	42	37
Shams Abad	2001//25	46	40	49.8	22
Almas	1984//7	60	42	49	10
	1996//7	65	12.4	21	15
Samian	1996//5	44	31	41	37
	2001//25	48	28	44.8	35
MeshkinShahr	1998//14	48	41	34	26.5

The results shown in Table 4 indicate that American Water Resources Association and 3×SD±M methods had the best efficiency by detecting 5 real outliers and not detecting unreal outliers. Moreover, Grubbs' Test and Box-Whisker Plot were more efficient in detection of high outliers than low outliers; however, these methods suffered from unreal outliers. Furthermore, Mahalanobis Distance was the least efficient method among others.

Table 4: comparison of efficiency of outlier detection methods for maximum daily rainfall in the stations

	Number of outliers			True percentage			Unreal outliers		
Outlier detection methods	High outlier	Low outlier	Total	High outlier	Low outlier	Total	High outlier	Low outlier	Total
3×SD±M	1	4	5	%100	%100	%100	0	0	0
Box-Whisker Plot	9	3	12	%100	%75	%80	6	0	6
American Water Resources Association	1	4	5	%100	%100	%100	0	0	0
Grubbs' test	6	1	7	%100	%25	%50	5	1	6
Mahalanobis Distance	5	2	7	%0	%50	%20	5	1	6

# CONCLUSION

With regard to the fact that maximum daily rainfall data is one of the most useful data for designing water structures as well as water and soil conservation programs, outlier detection is one of crucial stages in the relative studies and whatever kind of error in outlier detection will lead to unreal predictions and estimations in designs and simulations. Maximum rainfall data outliers lead to overestimation and consequently, higher design and water and soil conservation costs. On the other hand, if the historical outliers are eliminated,

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